

Spillover as Rational Processing Delay in Sentence Comprehension



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Traditional View: *Spillover* is typically treated as a byproduct of modular processing [1,2].

Our Proposal: It can instead arise from *rational* decisions to delay processing under memory constraints.

Prediction: The **benefit** of this delay, quantified by *mutual information* (MI) between W_i and $W_{>i}$, will be correlated with spillovers. → clear correlations found in three reading-time (RT) datasets.

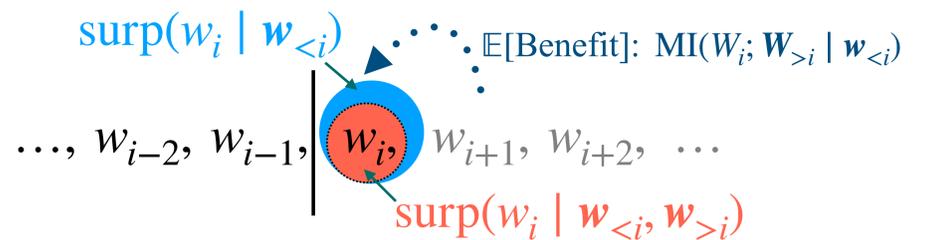
Proposal

- Sentence comprehension is incremental at a *macro* level but not necessarily fully incremental at a *micro* level.
 - Delayed integration: Comprehenders often wait for subsequent input.
 - Reduced surprisal: Integrating words in a richer context lowers processing difficulty.
- Expected benefit of processing delay is quantified by the mutual information between W_i and $W_{>i}$.

$$\Delta \overleftarrow{\text{surp}}_{w_i} := \text{surp}(w_i | \mathbf{w}_{<i}) - \text{surp}(w_i | \mathbf{w}_{<i}, \mathbf{w}_{>i})$$

$$= \text{pmi}(w_i; \mathbf{w}_{>i} | \mathbf{w}_{<i})$$

$$\mathbb{E}_{w_i | \mathbf{w}_{<i}} \left[\mathbb{E}_{\mathbf{w}_{>i} | \mathbf{w}_{<i}, w_i} [\Delta \overleftarrow{\text{surp}}_{w_i}] \right] = \text{MI}(W_i; W_{>i} | \mathbf{w}_{<i})$$



- Prediction: higher benefit at w_i should be associated with greater spillover at w_{i+1} .

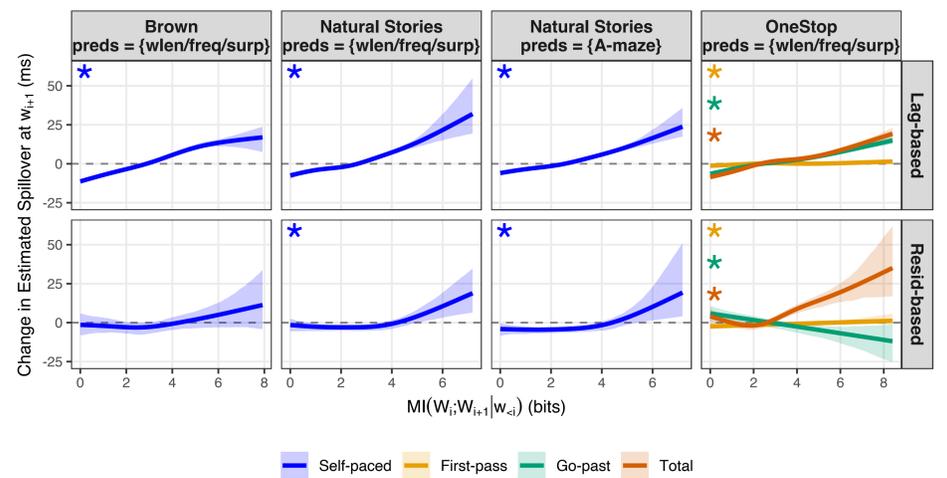
Analysis

Estimating word-by-word spillovers

- Two ways of estimating *relative* spillover on Brown [3], Natural Stories [4], and OneStop [5]:
 - 1) **Lag-based:** spillover as the contributions of lag predictors
 - Train: $\text{RT}(w_i) \sim \text{GAM}_\theta(\text{pred}(w_i) + \text{pred}(w_{i-1:i-3}))$
 - Predict: $\text{Spillover}_{\text{lag}}(w_i) = \sum_{w \in \text{heldout}} \text{GAM}_\theta(\text{pred}(w_{i-1:i-3}))$
 - 2) **Resid-based:** spillover as the residual of RT
 - Train: $\text{RT}(w_i) \sim \text{GAM}_\theta(\text{pred}(w_i))$
 - Predict: $\text{Spillover}_{\text{resid}}(w_i) = \text{RT}(w_i) - \text{GAM}_\theta(\text{pred}(w_i))$
- Two types of $\text{pred}(w_i)$ are used:
 - a) $\text{wlen}(w_i) + \text{freq}(w_i) + \text{surp}(w_i)$
 - b) $\text{A-maze}(w_i)$ (for Natural Stories [6])

Relationship between MI and spillovers

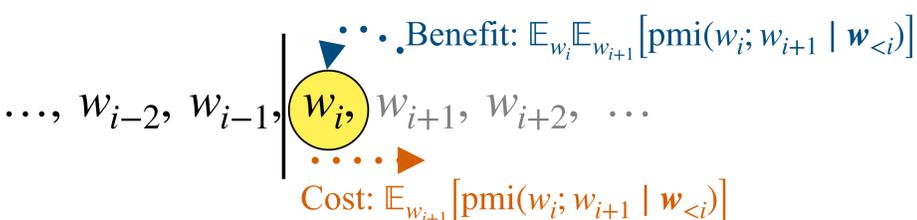
- Bootstrapped GAM smooths relating MI at w_i to estimated relative spillover at w_{i+1} .



Next Step

Benefit/cost tradeoff of processing delay

- Developing a *rational* framework to balance the *benefits* and *costs* of processing delays.
 - A temporal extension of surprisal theory.
 - Target phenomena: spillover, deep/shallow processing, reanalysis, and relative clause, ...



Information-theoretic storage cost

Information-Theoretic Storage Cost in Sentence Comprehension

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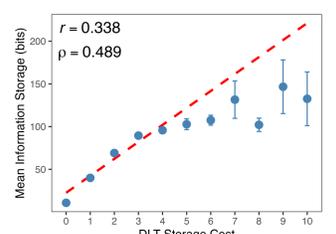
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- Maintaining information in working memory consumes cognitive resources.
- Our proposal: An information-theoretic formulation of this storage cost

$$\mathbb{E}_{w_{[k:N]} | w_{[1:k]}} [\text{pmi}(w_i; w_{[k:N]} | w_{[1:k] \setminus i})]$$



Correlation between DLT storage and information storage in the UD_English-GUM

References:

- [1] Mitchell (1984) [2] Bartek et al. (2011) [3] Smith & Levy (2013)
 [4] Futrell et al. (2021) [5] Berzak et al. (2025) [6] Boyce & Levy (2023)

$$\text{InfoStor}_k := \sum_{i=1}^{k-1} \mathbb{E}_{w_{[k:N]} | w_{[1:k]}} [\text{pmi}(w_i; w_{[k:N]} | w_{[1:k] \setminus i})]$$