

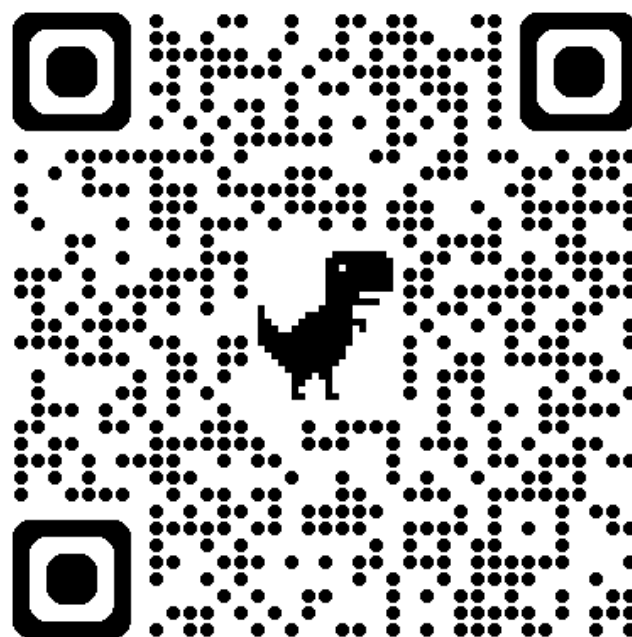


Information-Theoretic Storage Cost in Sentence Comprehension

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Georgetown

Shinnosuke Isono
NINJAL

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Georgetown



← Our paper 🙄🙄

Background

Storage Cost during Comprehension

- Comprehenders maintain incoming words to anticipate future input.

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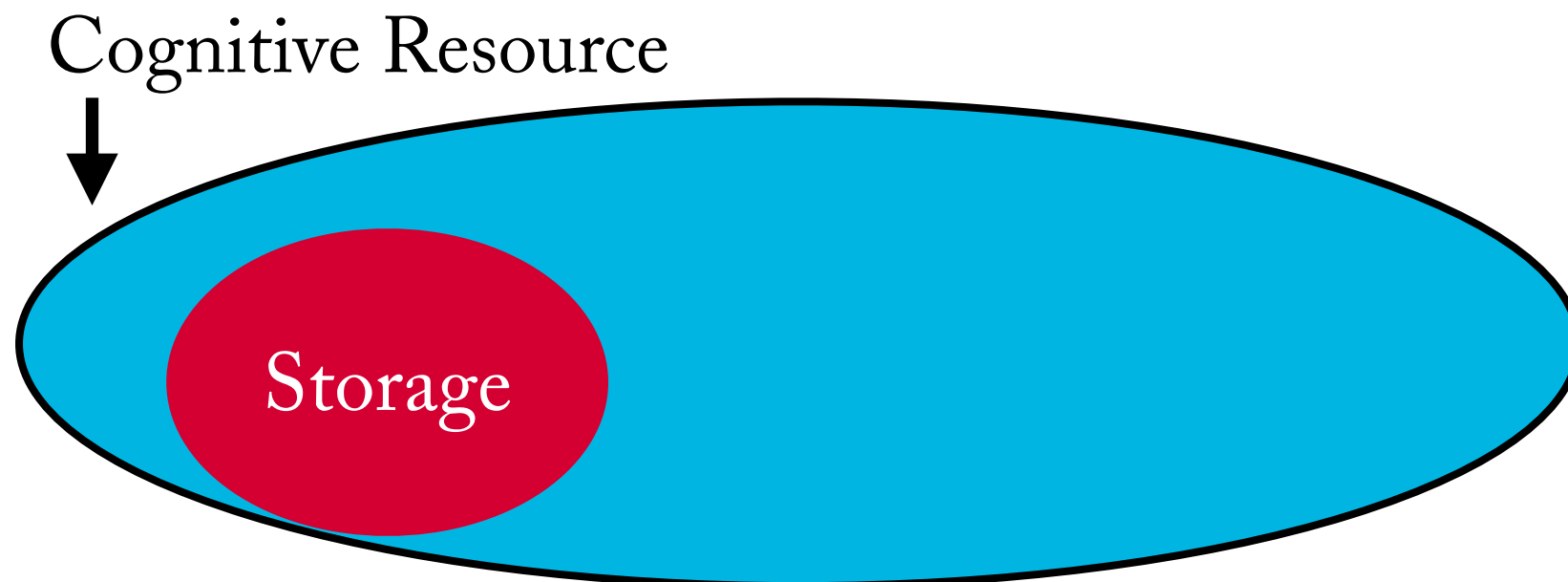
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 - Accumulated predictions consume memory resources and create a processing bottleneck [Just & Carpenter 1992]

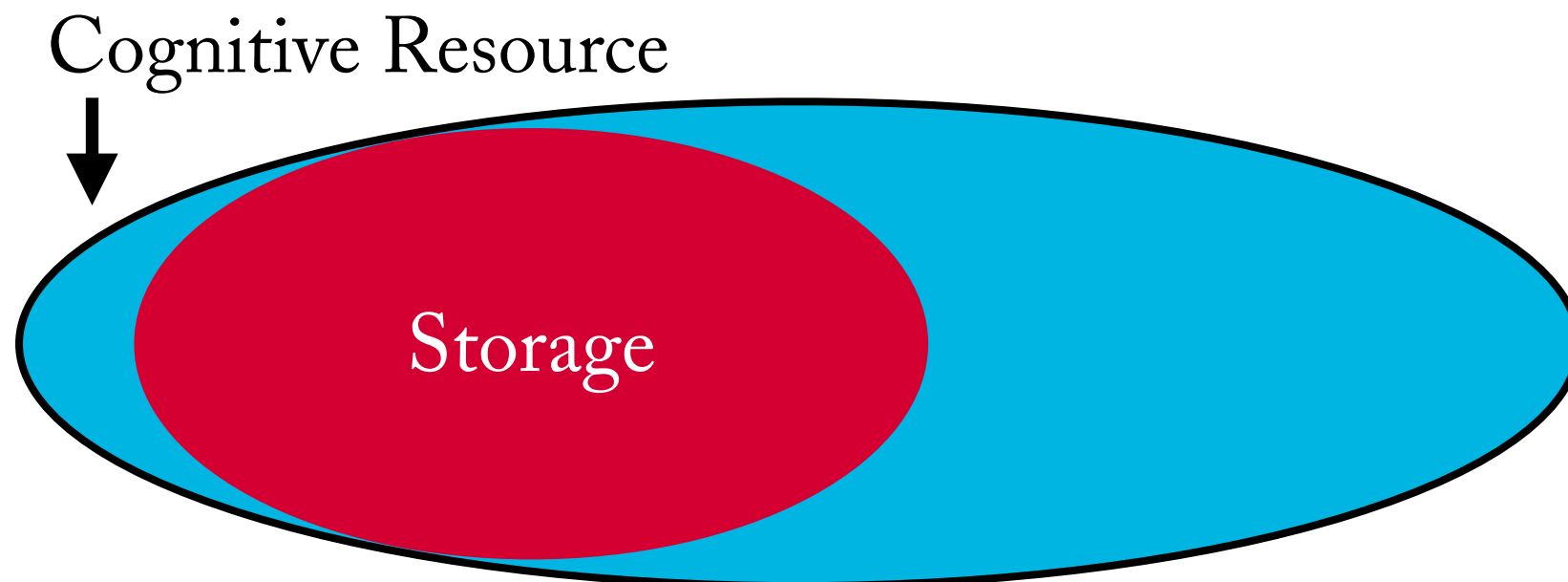


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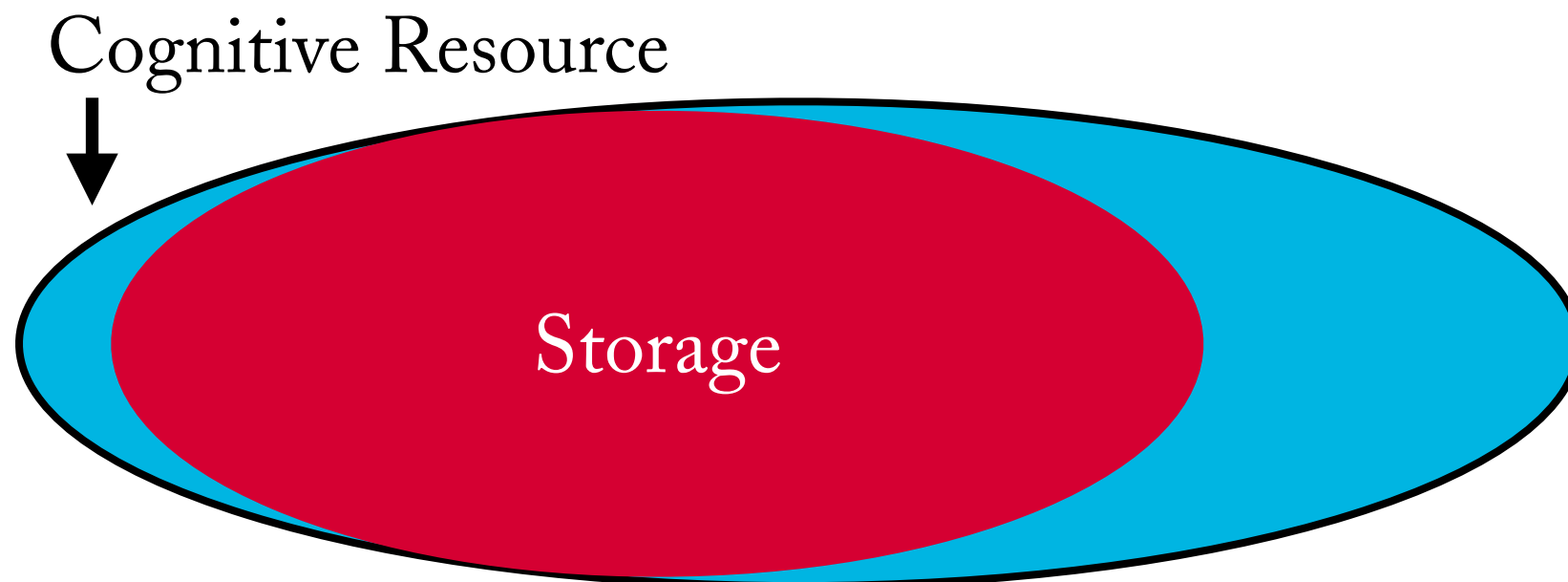


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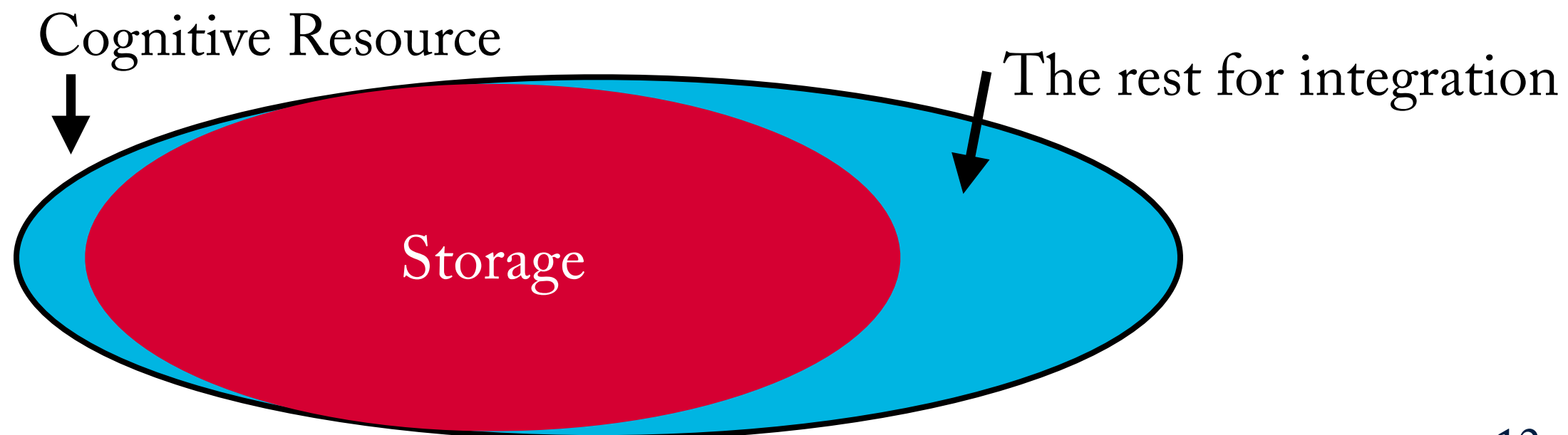


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[Yngve 1960; Miller & Chomsky 1963; Gibson 1998]

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How do we quantify the information in working memory?

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- Dependency Locality Theory (DLT; [Gibson 2000])
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- ➡ We address all of them by the *information-theoretic* reformulation.

Proposal

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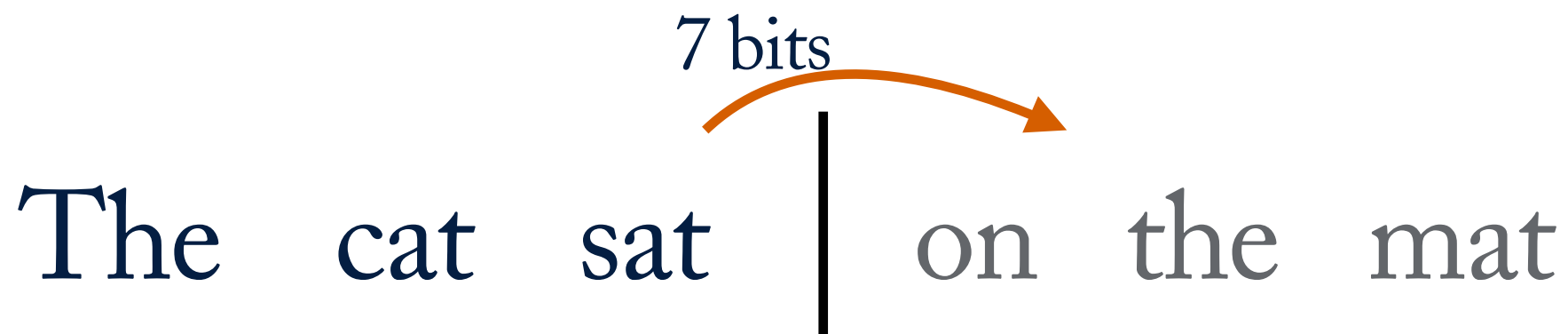
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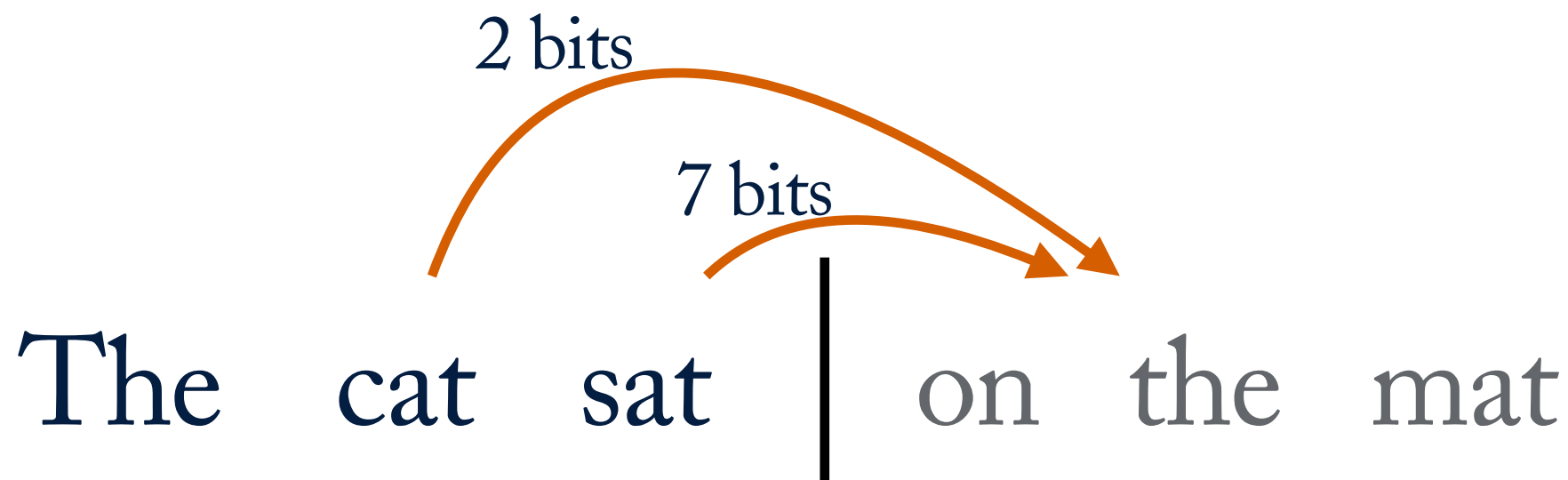
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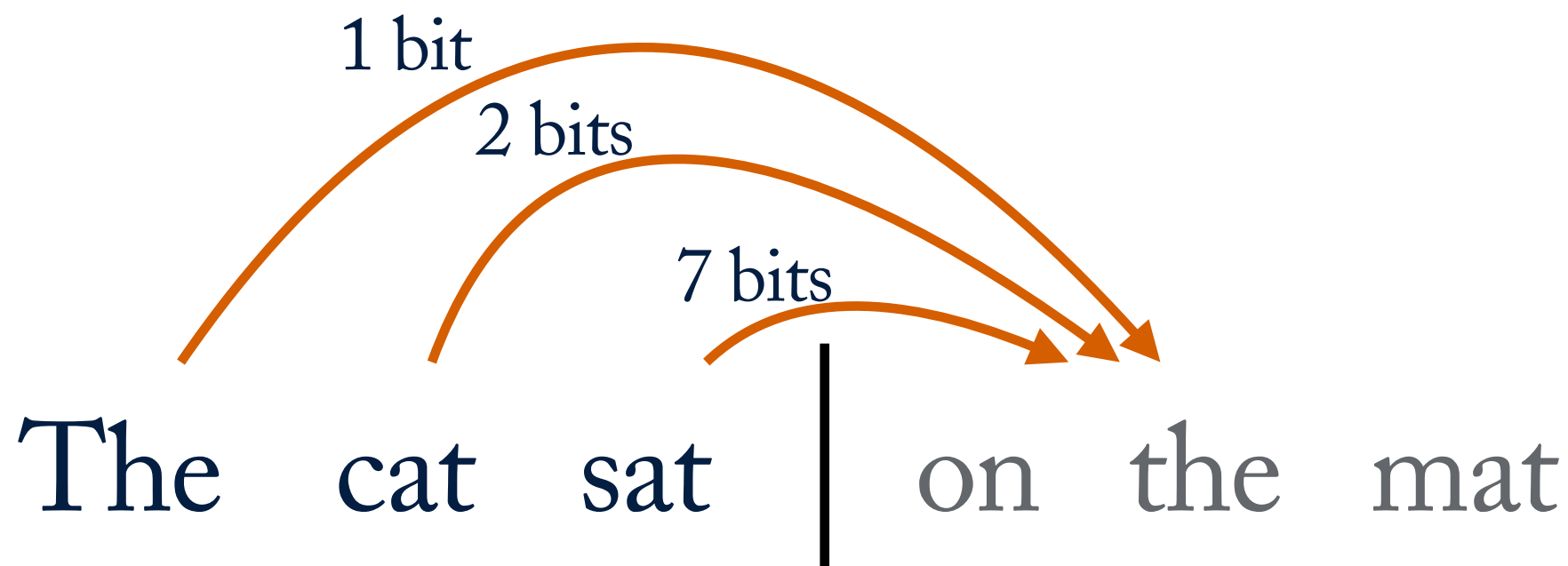
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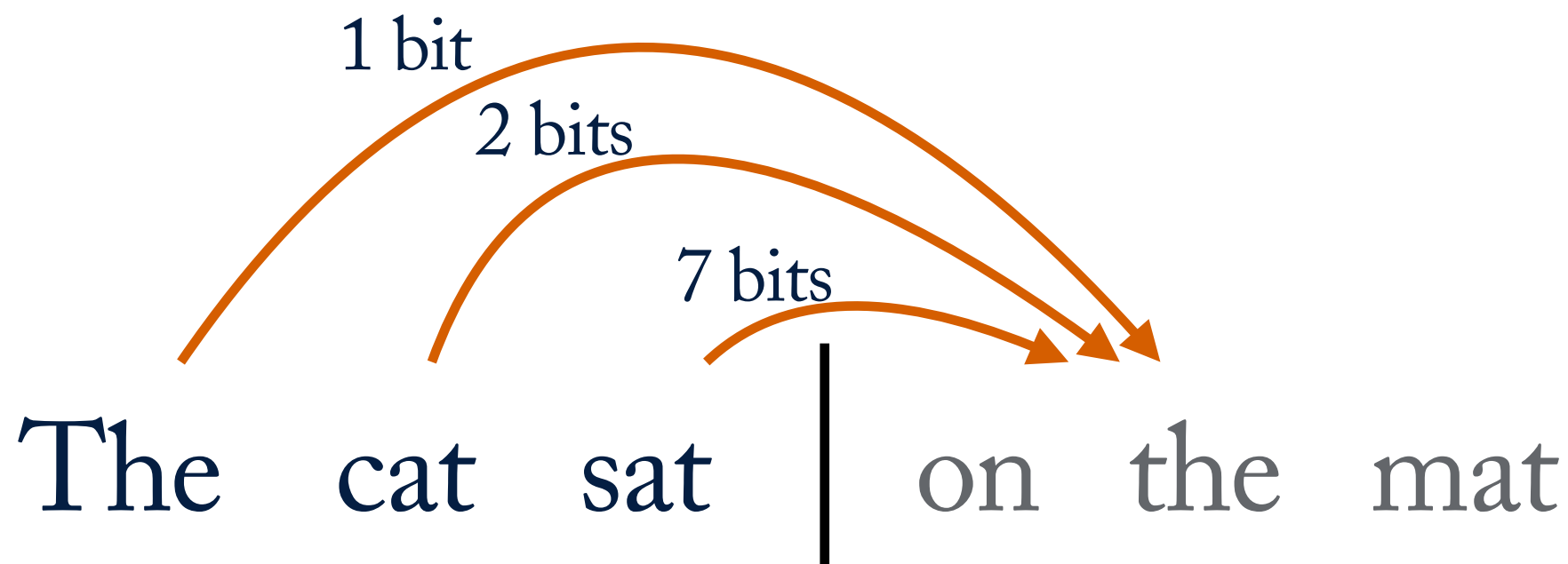
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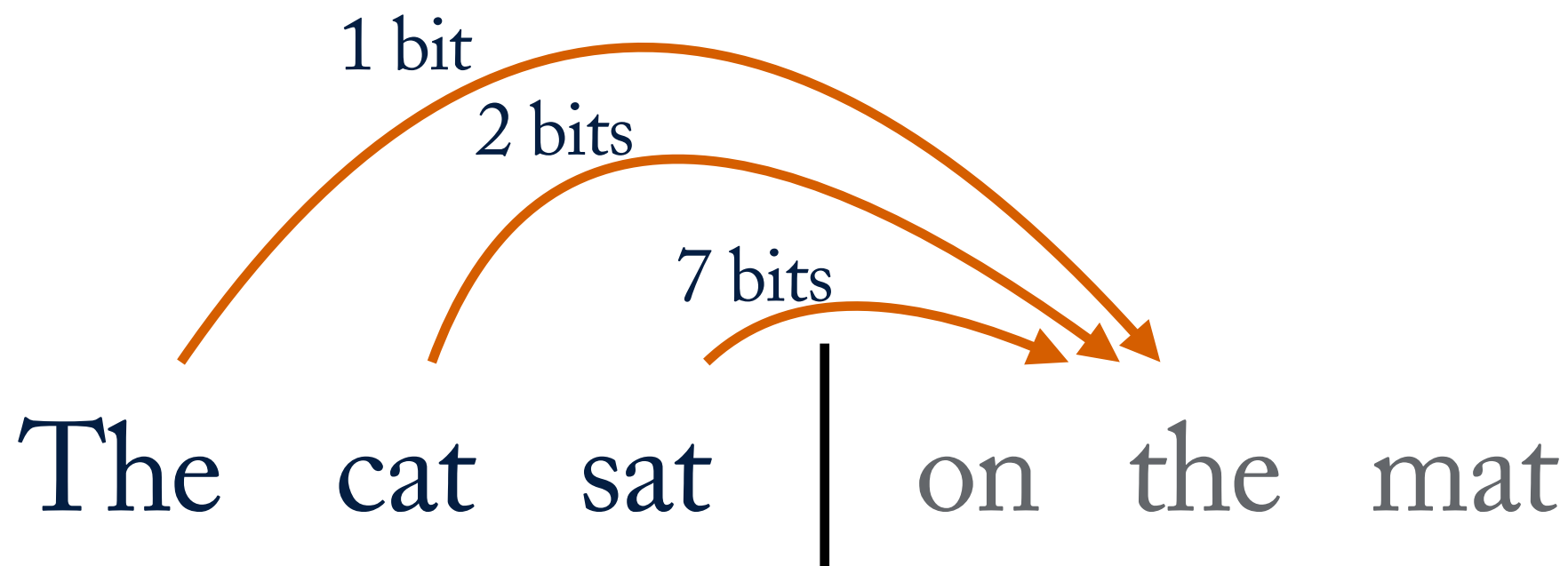
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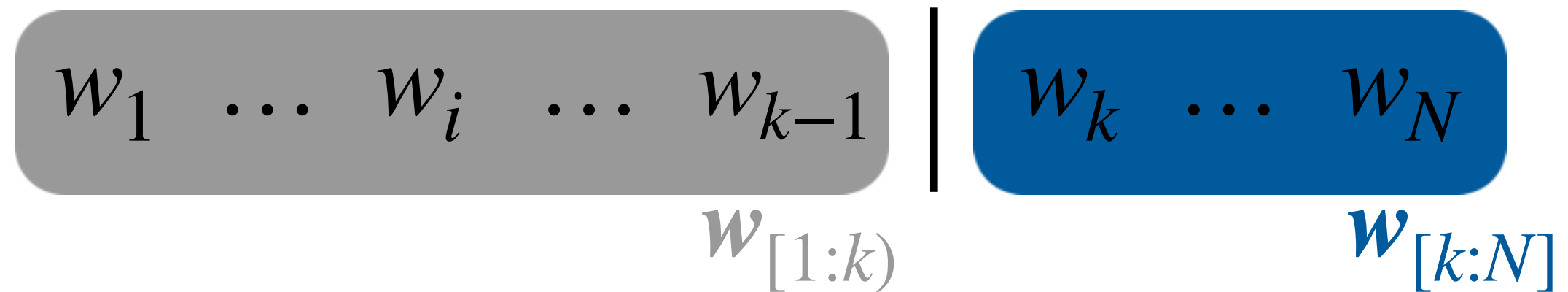
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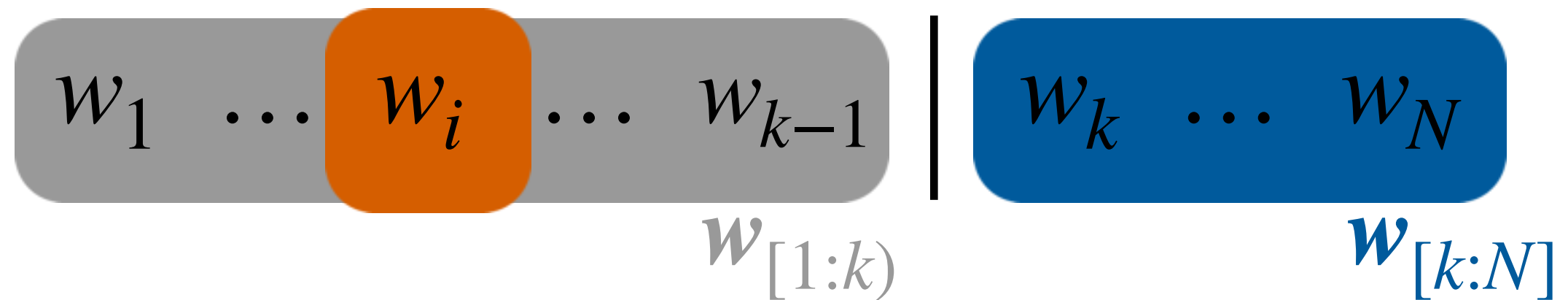
- Information storage at **on** is: $1 + 2 + 7 = 10$ bits

Information-theoretic Storage

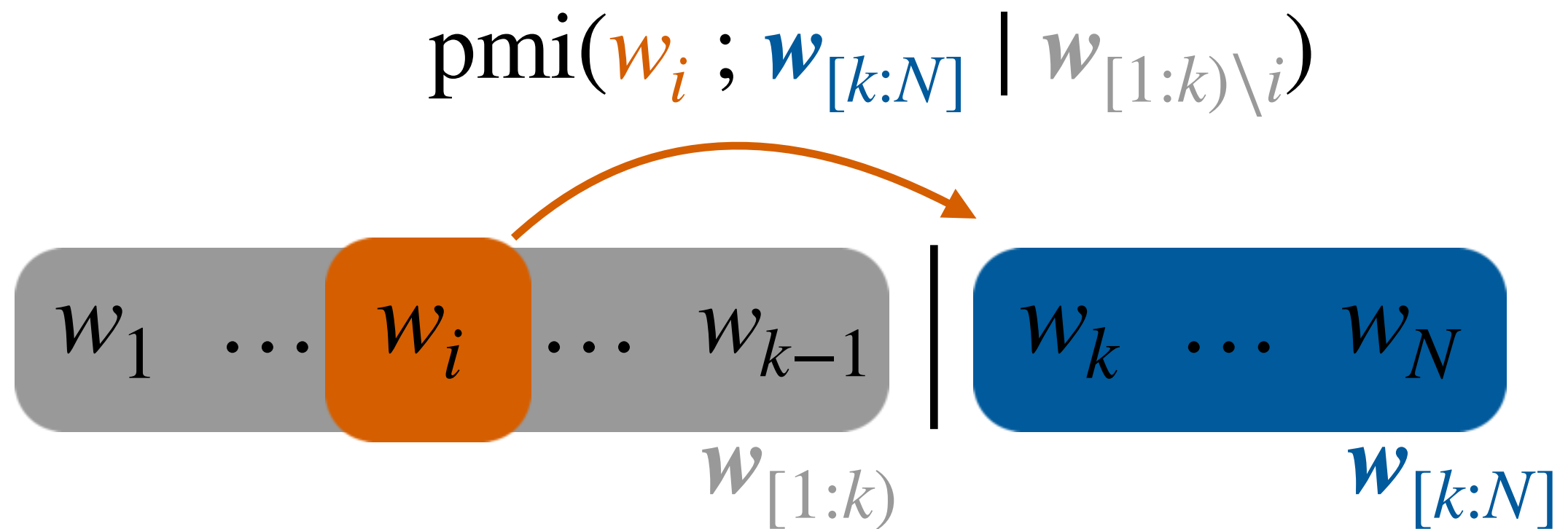
More formally ...



Information-theoretic Storage

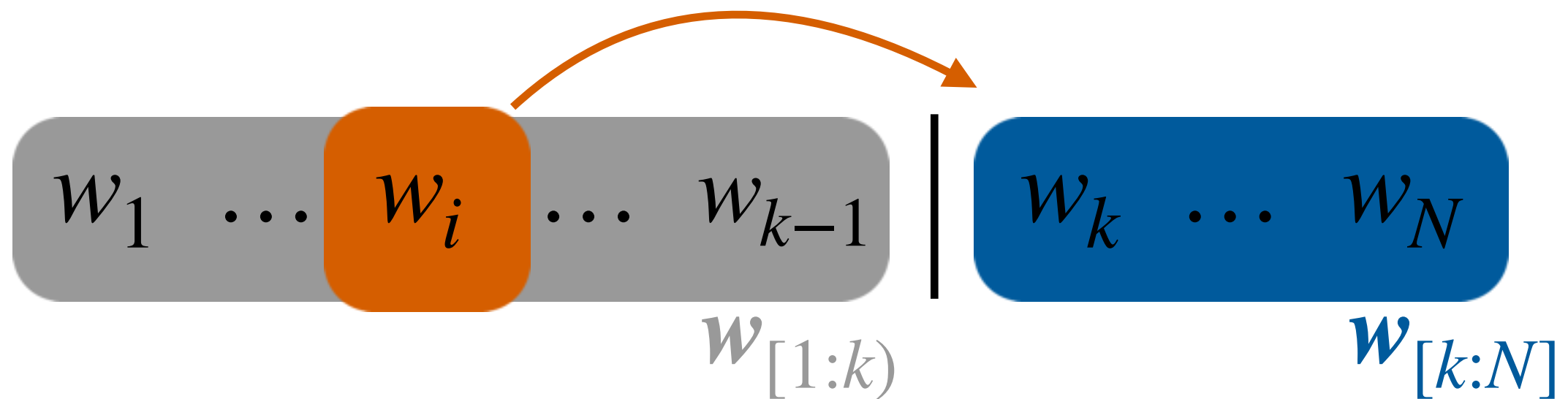


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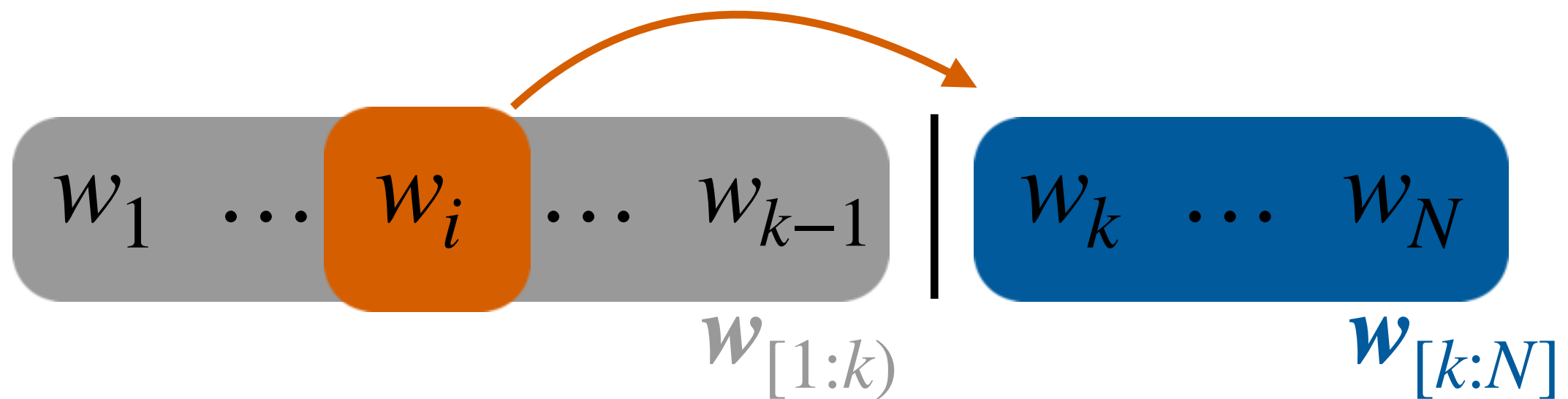
Information-theoretic Storage

$$\mathbb{E}_{\mathbf{w}_{[k:N]} | \mathbf{w}_{[1:k)}} [\text{pmi}(\mathbf{w}_i ; \mathbf{w}_{[k:N]} \mid \mathbf{w}_{[1:k)} \setminus i)]$$



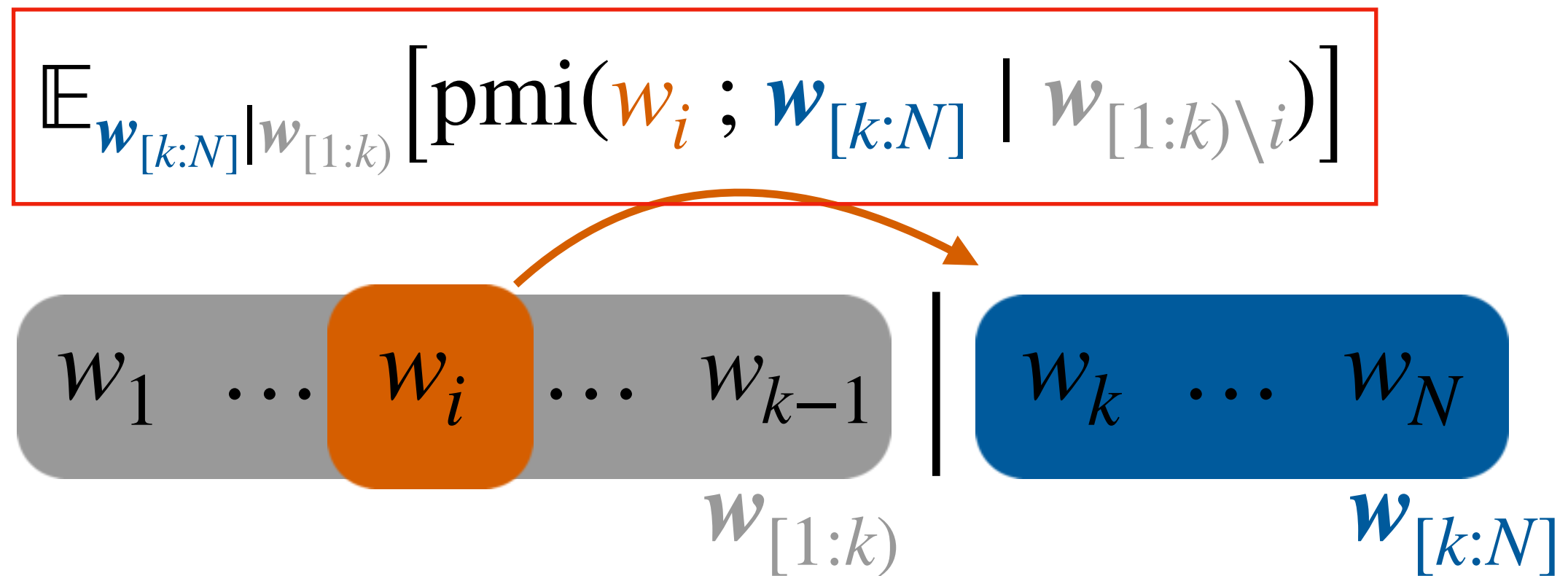
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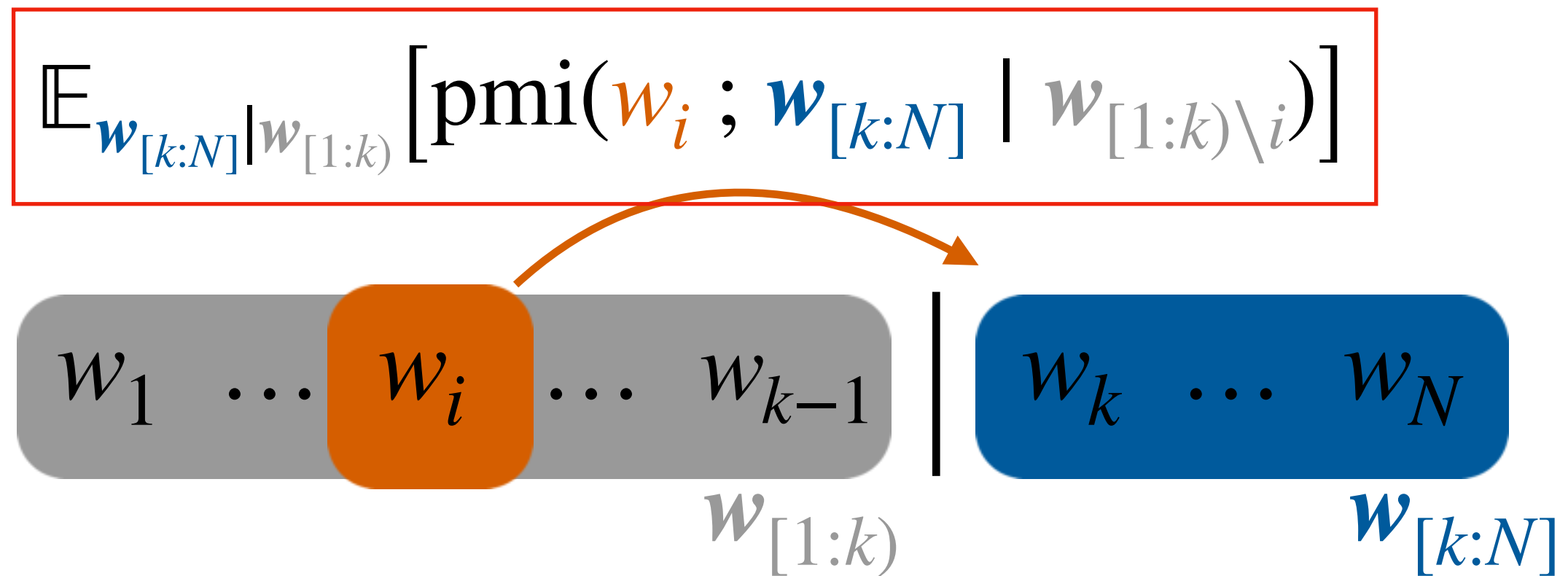
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- We estimated the expected PMI via BERT [Devlin+ 2019; Hoover+ 2021].

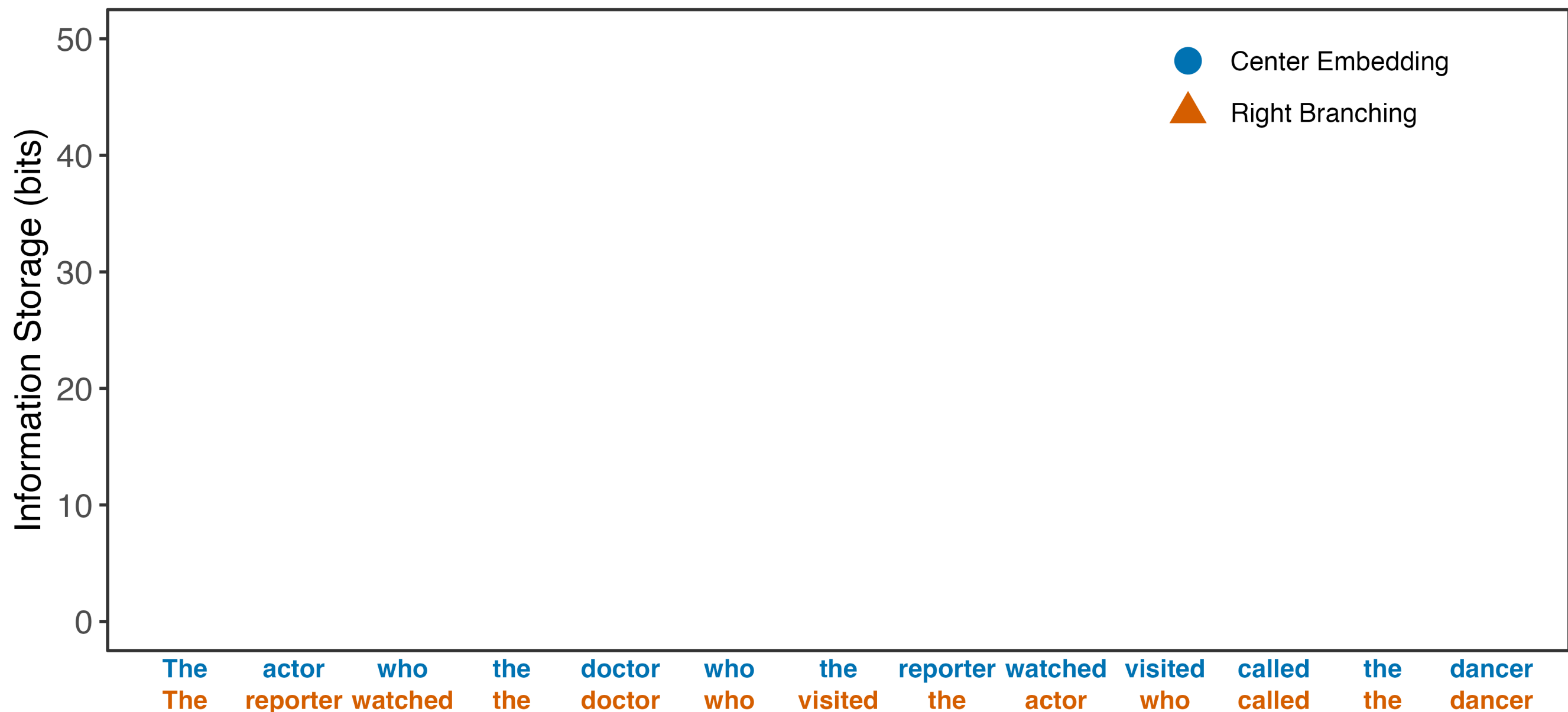
Experiments

1. Case Study: Center-embedding

- Processing difficulty: center-embedded > right-branching

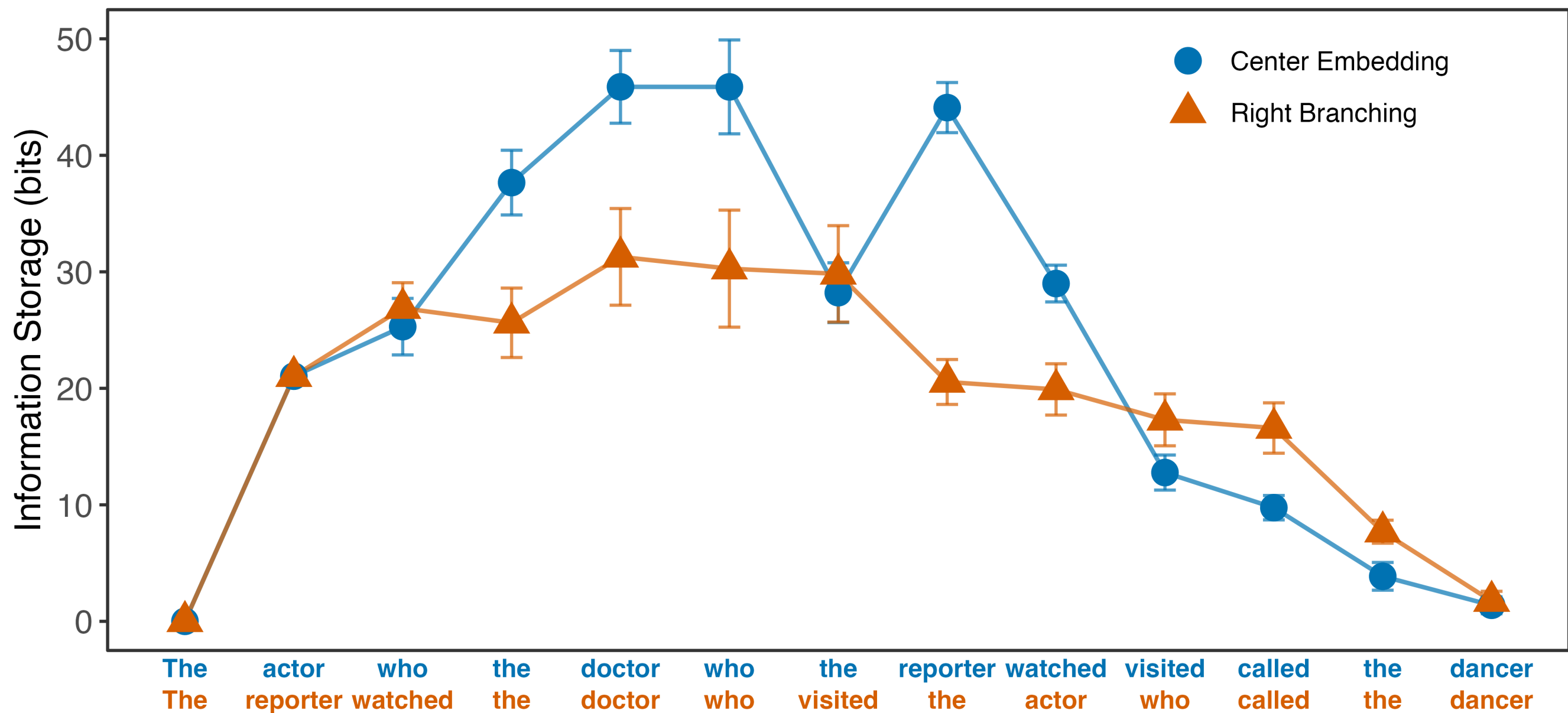
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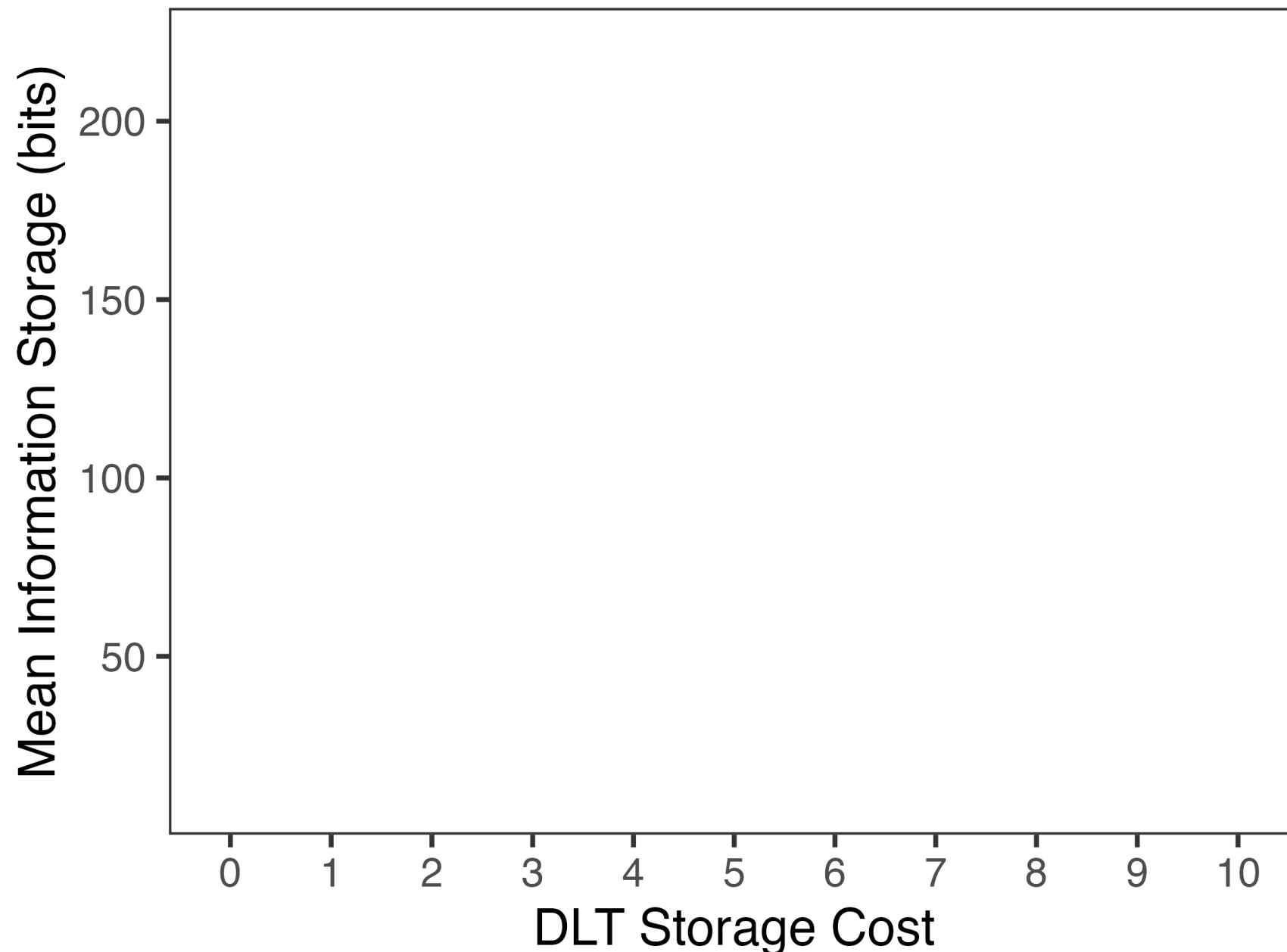
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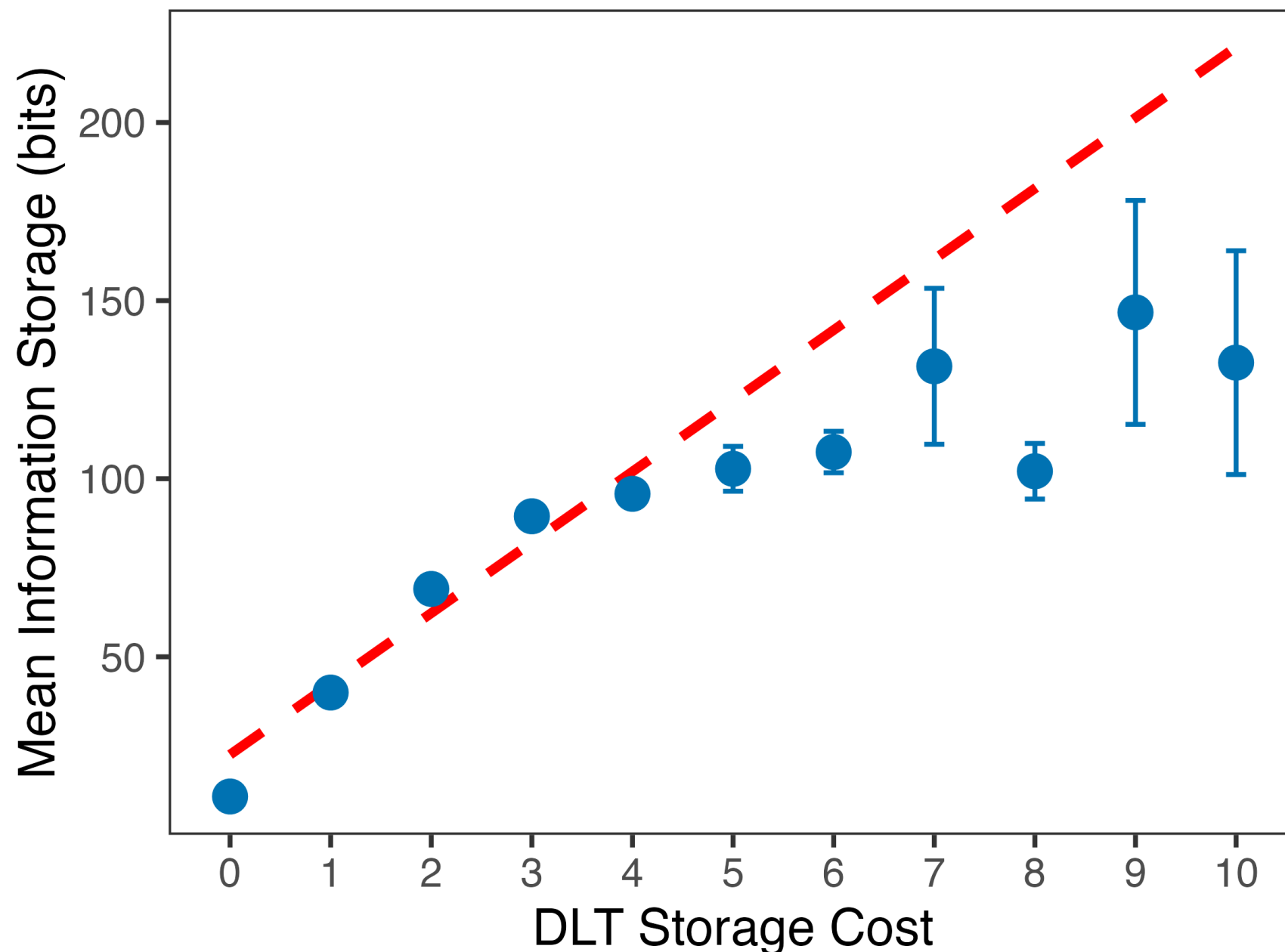
2. Correlation with DLT

- Is our Information Storage correlated with DLT storage?
 - Test in UD_English-GUM [Zeldes 2017] (233,926 words)



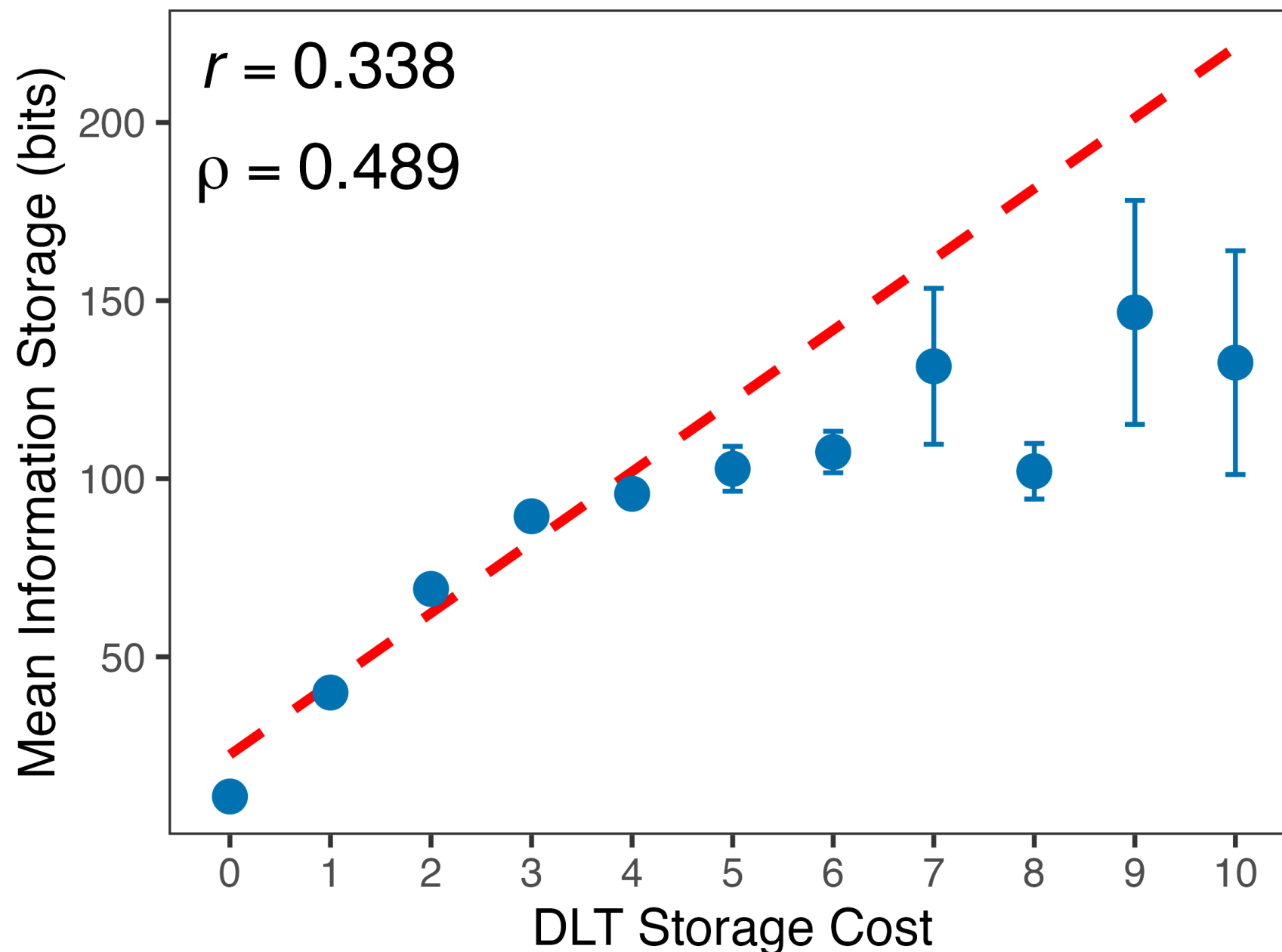
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from GPT-2
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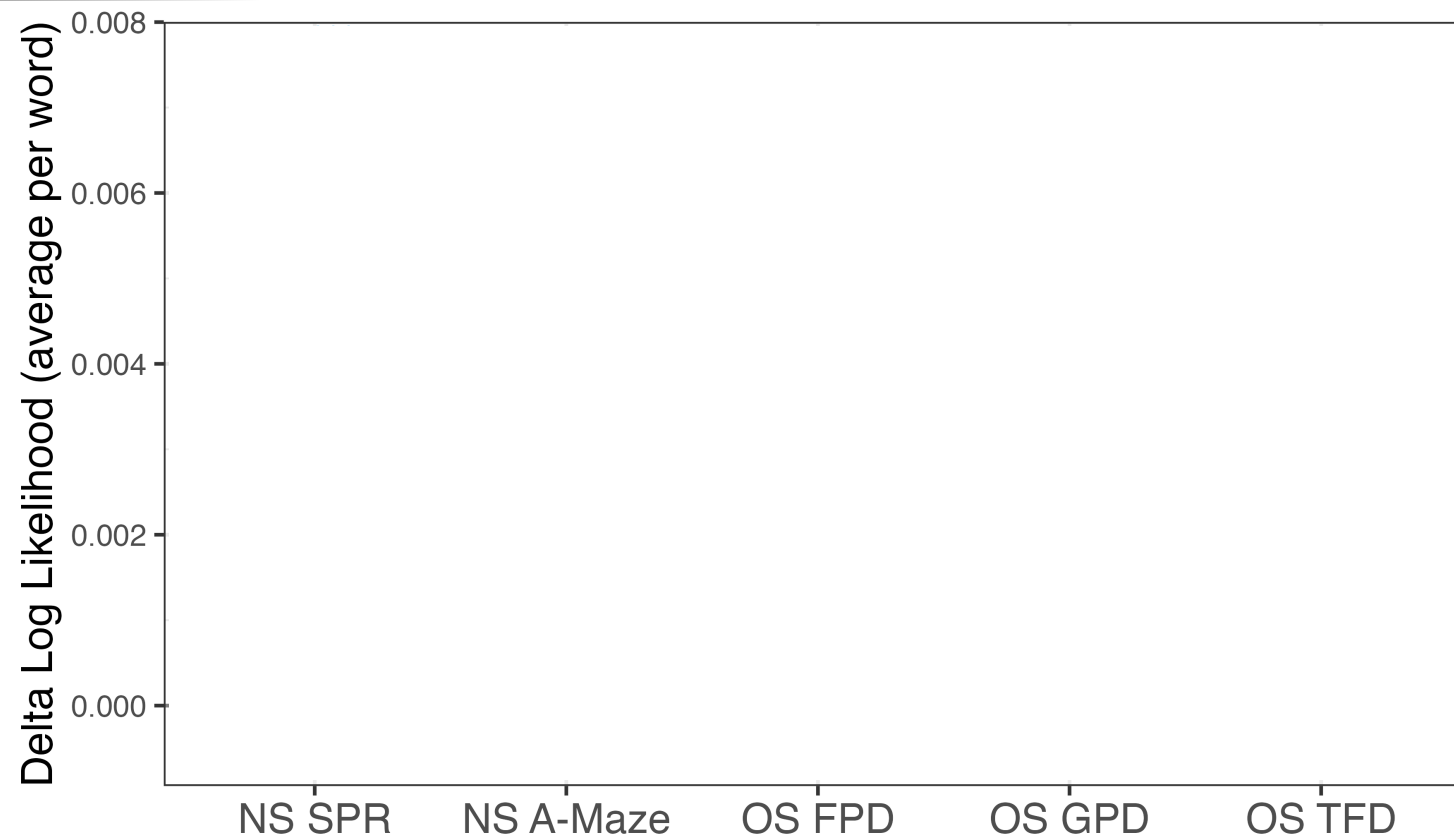
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- Test on the large-scale English datasets (<#subject>)
 - *Natural Stories* [Futrell+ 2021]
 - *OneStop* [Berzak+ 2025]
 - Self-paced reading (181) [Futrell+ 2021]
 - Eye-tracking (180)
 - A-maze reading (95) [Boyce & Levy 2023]

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● Info ▲ DLT ○ Info-on-DLT △ DLT-on-Info

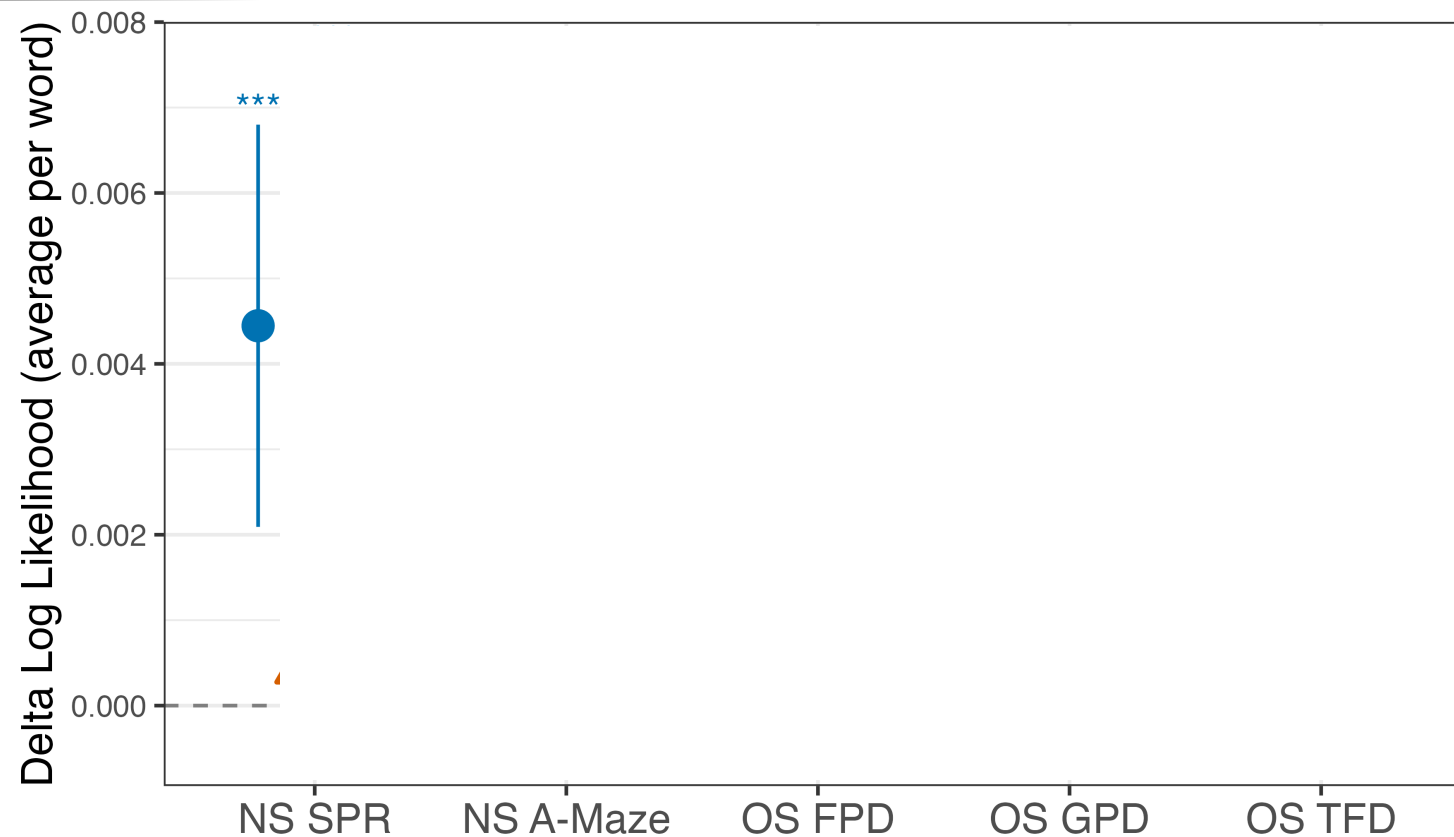
Just information storage cost

How much *more* reading-time variance is explained above DLT

NS=Natural Stories; OS=OneStop

SPR=self-paced reading; FPD=first-pass duration; GPD=go-past duration; TFD=total fixation duration

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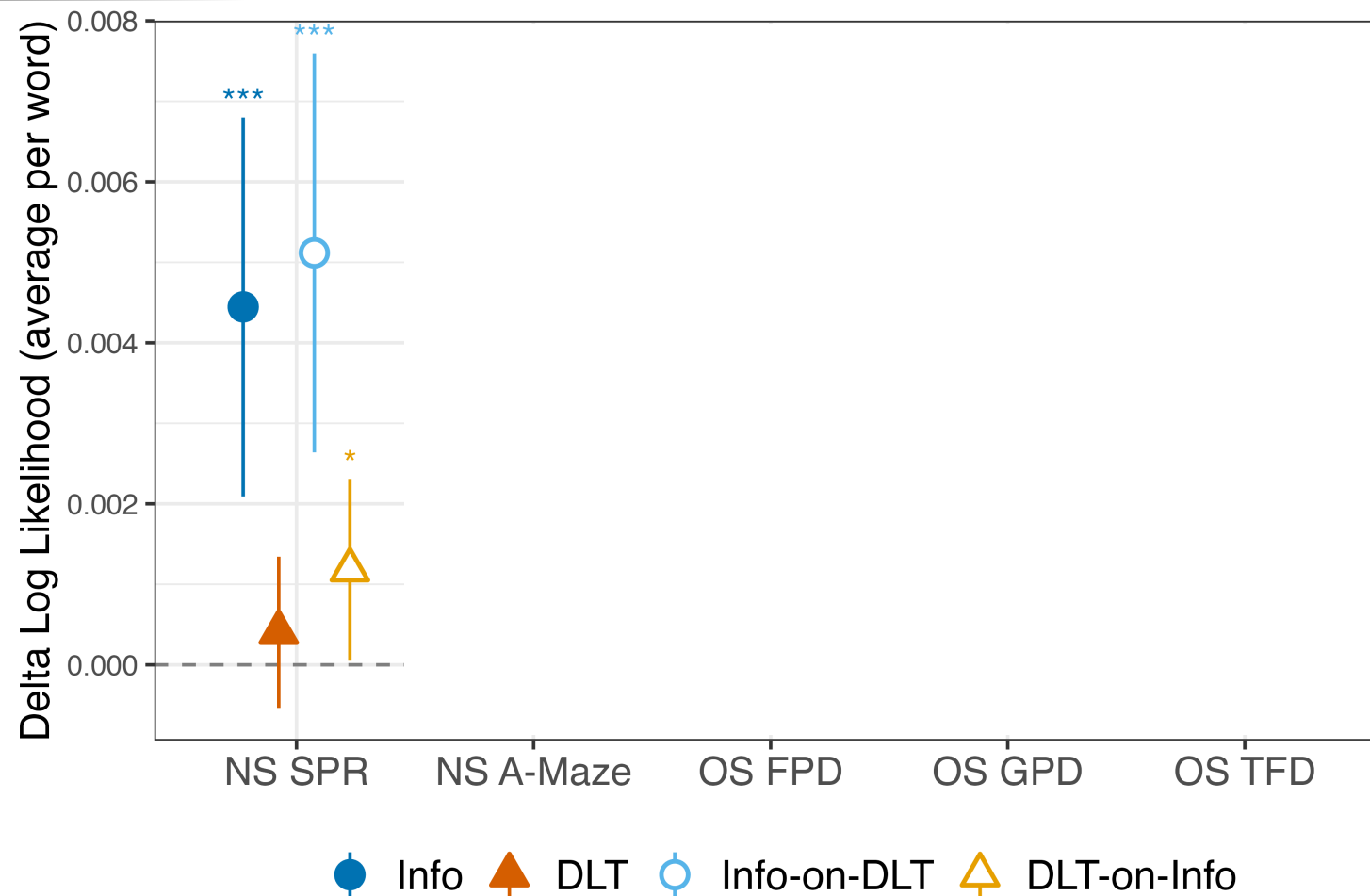
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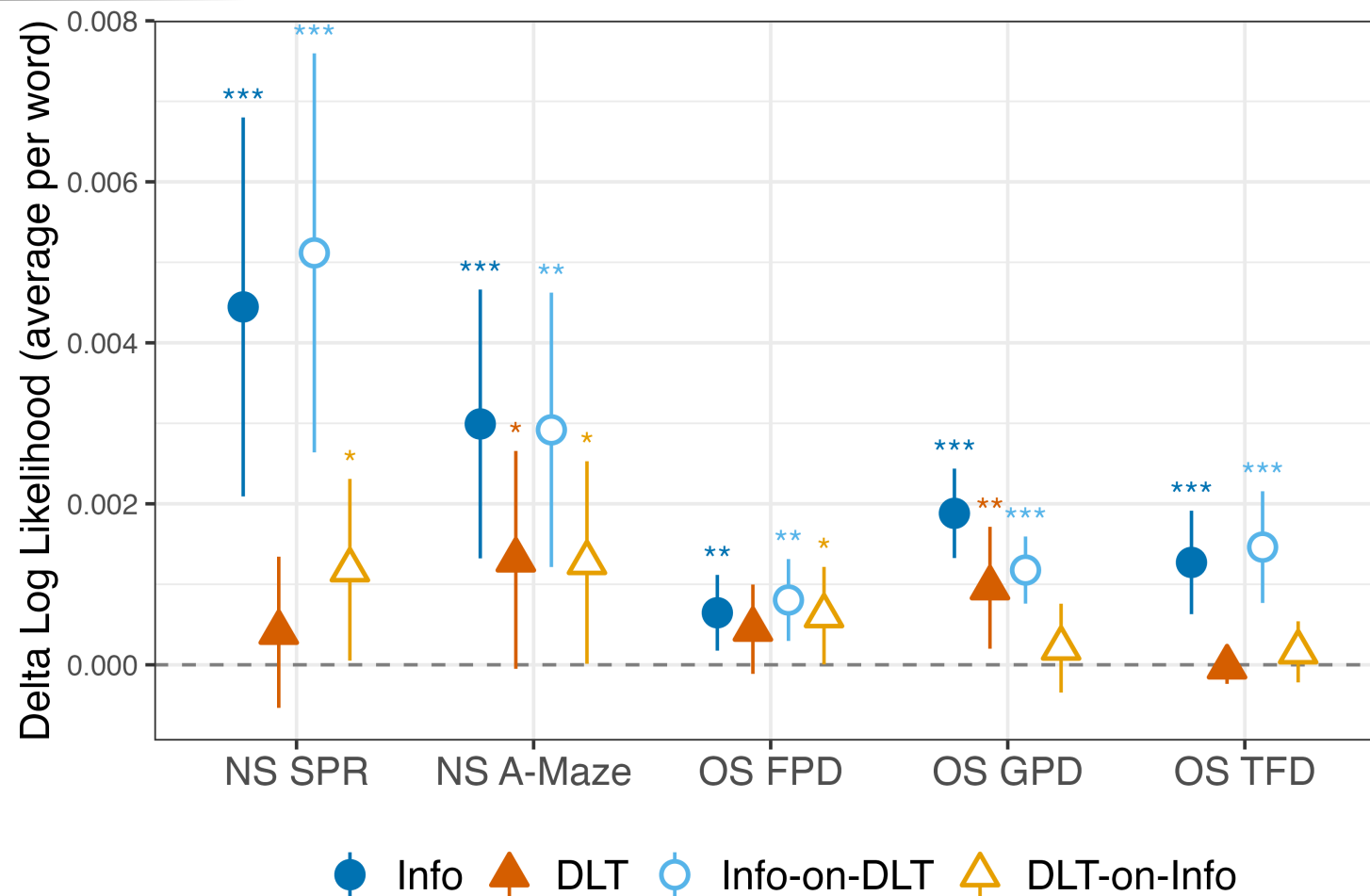
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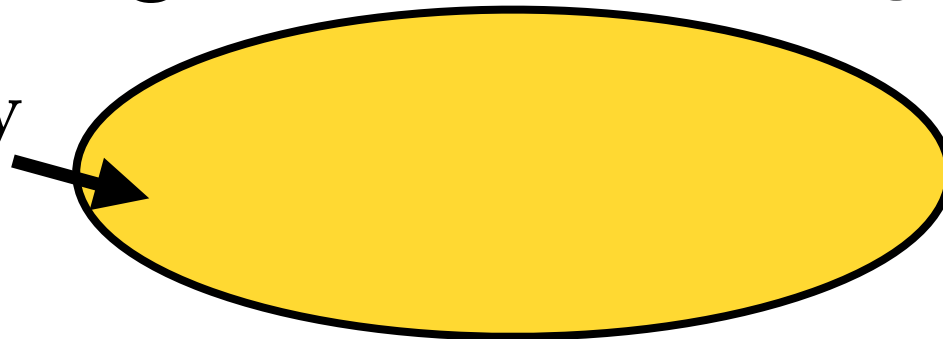
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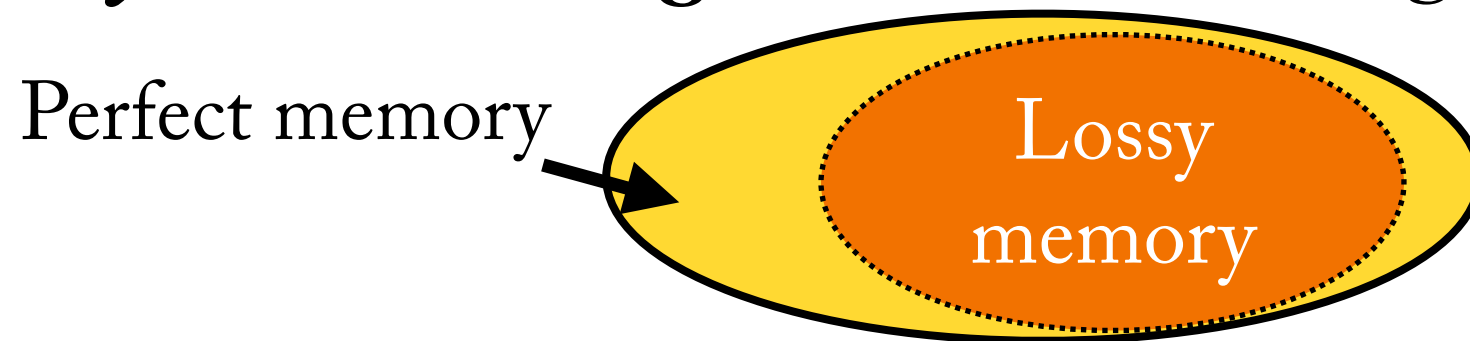
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 - Our framework provides a formal foundation to explore *lossy-context storage* under limited cognitive resources.

Perfect memory



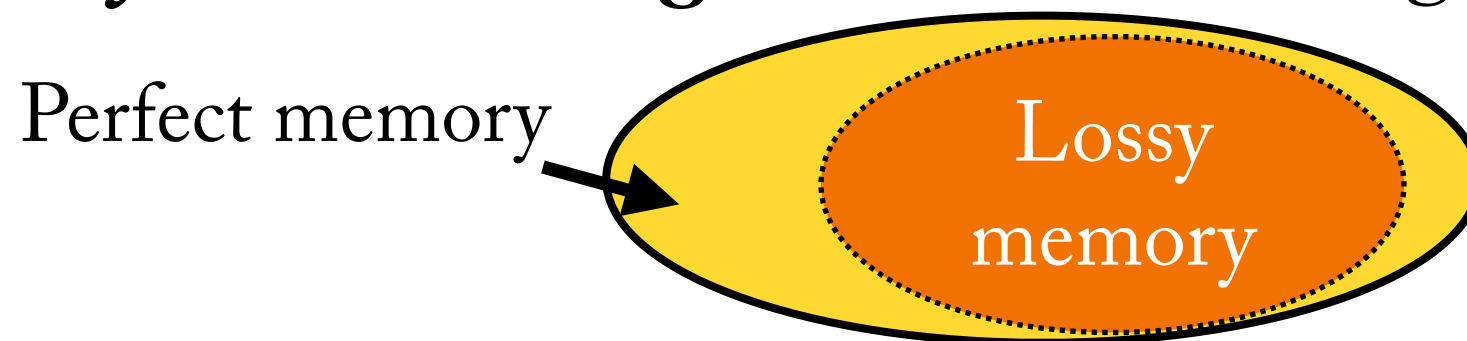
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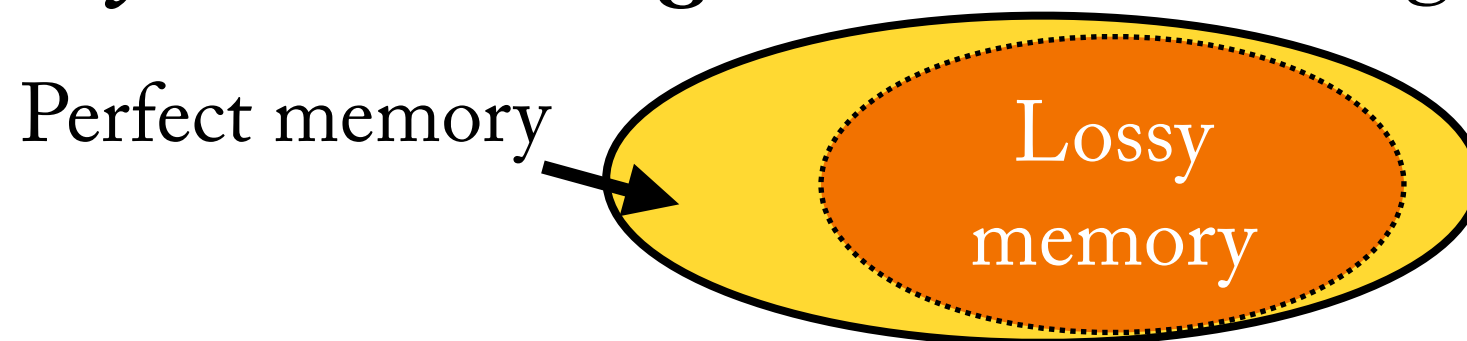
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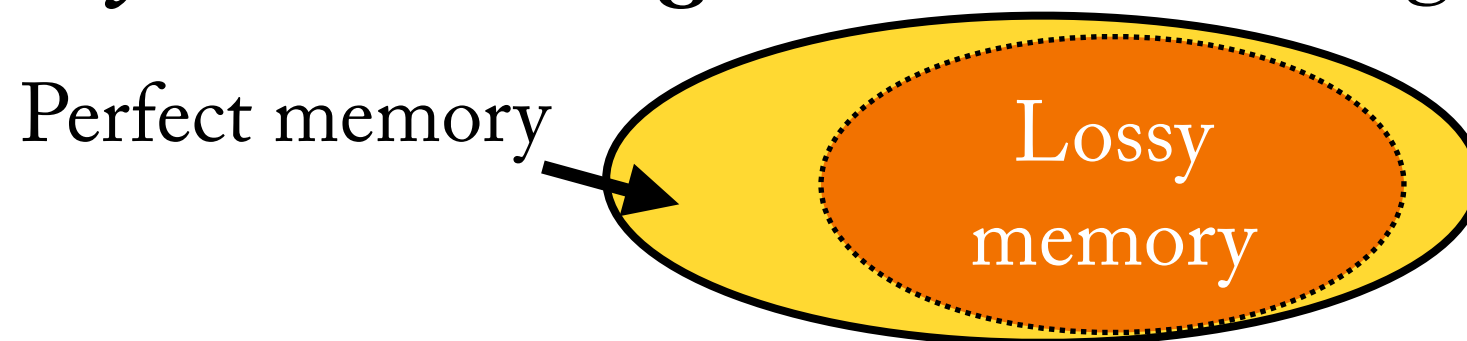
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 - **Statistical** prediction and **structural** processing operate as distinct, complementary mechanisms [Kajikawa & Isono 2026].

Discussion & Implications

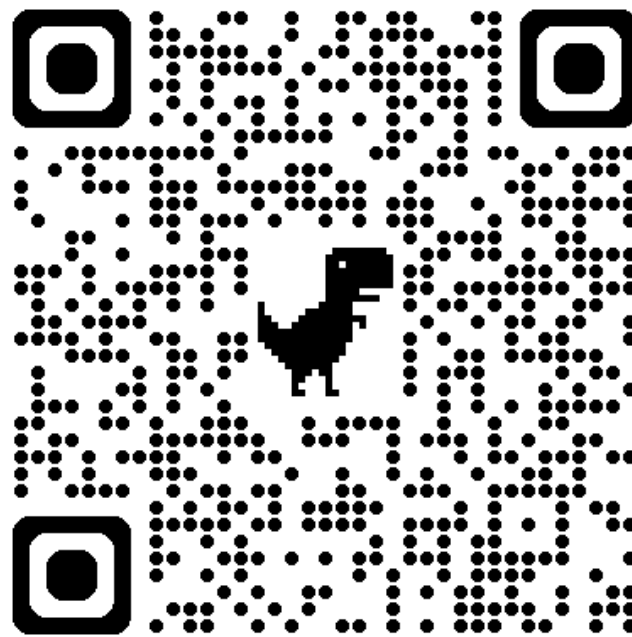
- Operationalized storage cost as (half-pointwise) mutual information between past and future.
 - Our framework provides a formal foundation to explore *lossy-context storage* under limited cognitive resources.



- Information/DLT storage capture distinct sources of reading-time variance.
 - **Statistical** prediction and **structural** processing operate as distinct, complementary mechanisms [Kajikawa & Isono 2026].
 - It might be better to assume **structured representation** rather than token sequences.

Thank you!!

- We proposed an *information-theoretic storage cost*
 - estimated from a neural language model without syntactic annotation
 - recovers well-known processing asymmetries to specific constructions
 - correlates with DLT storage
 - predicts naturalistic reading times



↑ Our paper 🙄🙄

Appendix

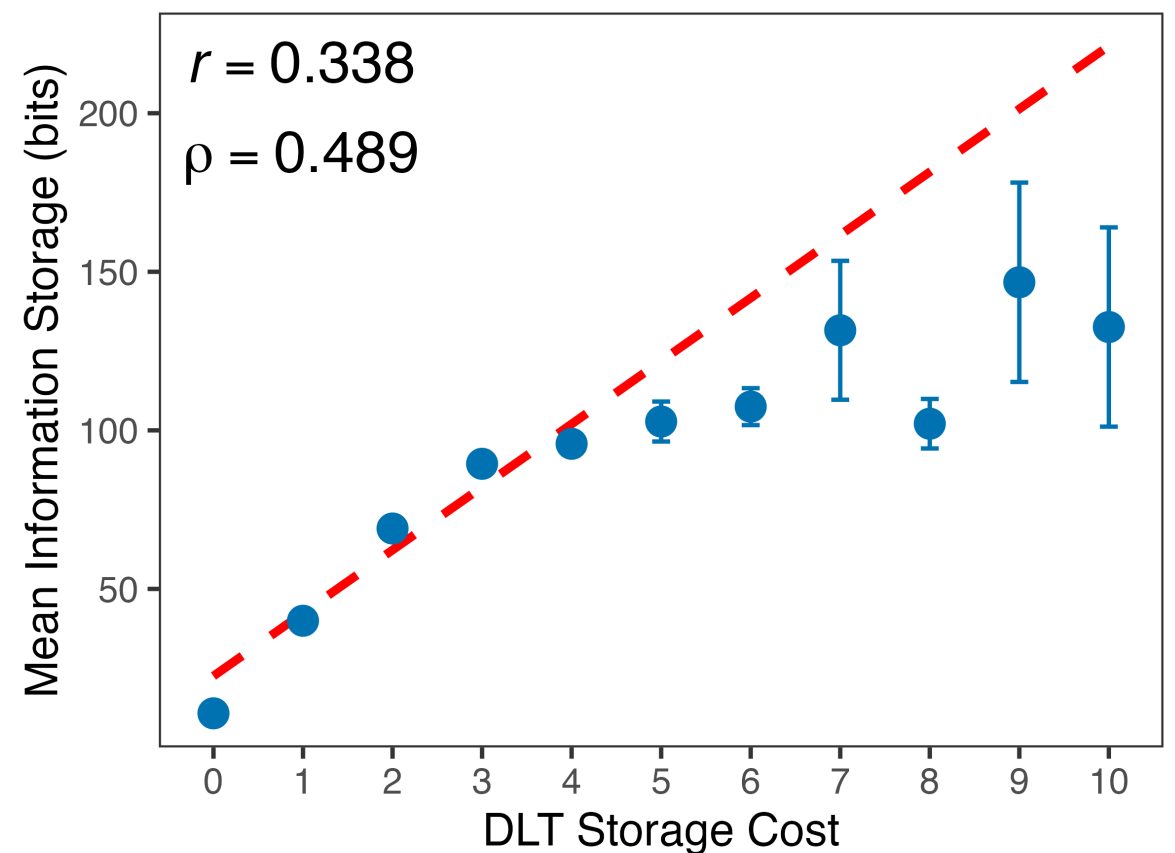
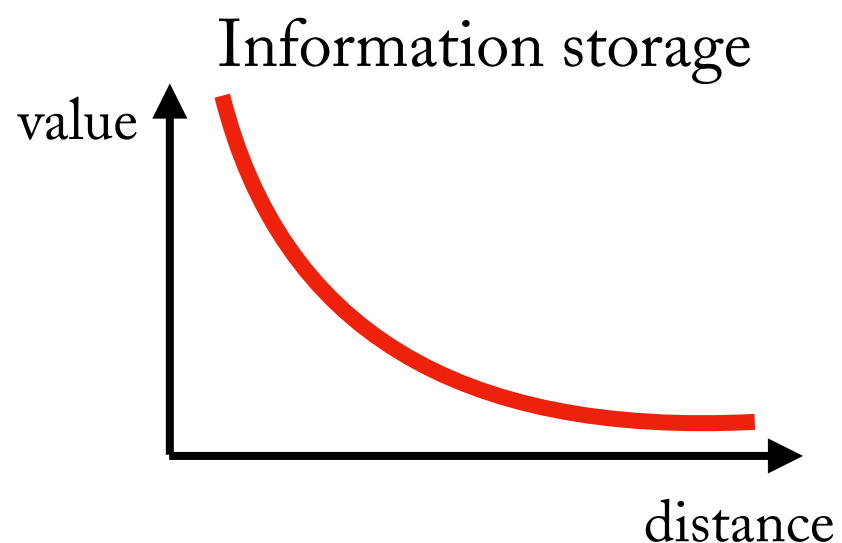
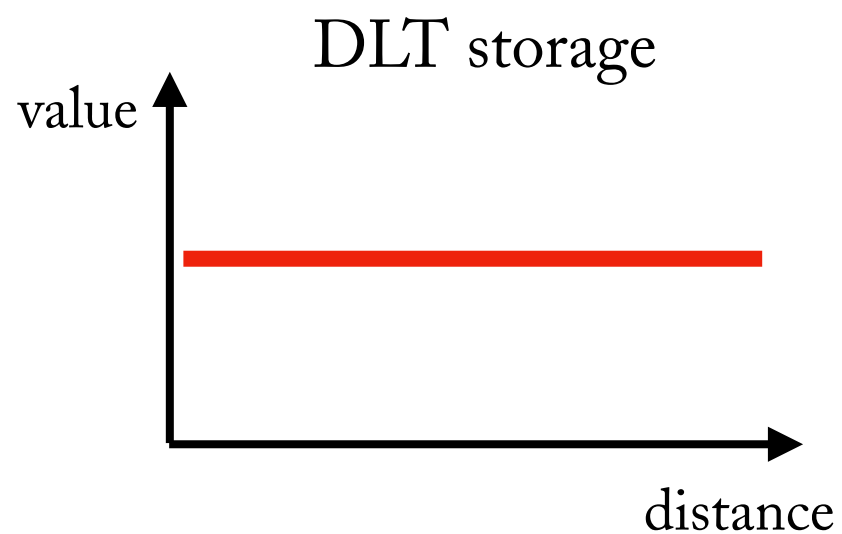
Estimation using BERT

$$\begin{aligned} \mathbb{E}_{\mathbf{w}_{[k:N]} | \mathbf{w}_{[1:k)}} [\text{pmi}(w_i; \mathbf{w}_{[k:N]} \mid \mathbf{w}_{[1:k)} \setminus i)] \\ = \text{KL} \left(\underbrace{p(\mathbf{W}_{[k:N]} \mid \mathbf{w}_{[1:k)})}_{\downarrow} \parallel \underbrace{p(\mathbf{W}_{[k:N]} \mid \mathbf{w}_{[1:k)} \setminus i)}_{\downarrow} \right) \end{aligned}$$
$$\mathbb{E}_W [\text{pmi}(\text{cat}; W \mid \text{The})] = \text{KL} (p(\textcolor{red}{[M]} \mid \text{The } \textcolor{blue}{\text{cat}}) \parallel p(\textcolor{red}{[M]} \mid \text{The } \textcolor{blue}{[M]}))$$

👁👁 Please refer to our paper for the estimation details
and the results of other BERT-family models

Why sublinear?

- The sub-linearity likely reflects a difference between the two metrics:
 - DLT storage increases *linearly* as it counts the number of unseen tokens
 - Information storage may not do so because mutual information in natural language decays according to a *power law* over distance [e.g., Debowski 2015; Hahn+ 2021]



Correlations between Predictors

- Pearson correlation matrix of predictors in Natural Stories

	position	wlen	wlen_so	unisurp	unisurp_so	gpt2_surp	gpt2_surp_so	dlt_stor	dlt_stor_so	info_stor	info_stor_so
zone	-0.01	0.01	0.00	0.01	0.00	-0.02	-0.02	0.00	0.00	-0.09	-0.09
position	0.00	0.01	0.00	-0.03	-0.02	-0.04	-0.10	-0.03	-0.12	-0.01	
wlen	-0.06	0.67	-0.07	0.50	-0.06	0.03	-0.02	0.08	0.07		
wlen_so	-0.07	0.67	-0.07	0.48	0.00	0.14	0.06	0.11			
unisurp	-0.07	0.53	-0.05	0.09	0.01	0.07	0.04				
unisurp_so	-0.04	0.52	-0.01	0.20	0.02	0.06					
gpt2_surp	-0.03	0.11	-0.03	0.01	0.01						
gpt2_surp_so	0.03	0.16	0.02	-0.02							
dlt_stor	0.61	0.23	0.22								
dlt_stor_so	0.21	0.22									
info_stor	0.85										

- zone: word position in a document
- position: word position in a sentence
- wlen: word length
- unisurp: unigram surprisal
- gpt2_surp: GPT-2 surprisal
- dlt_stor: DLT storage cost
- info_stor: Information storage cost
- _so: spillover region